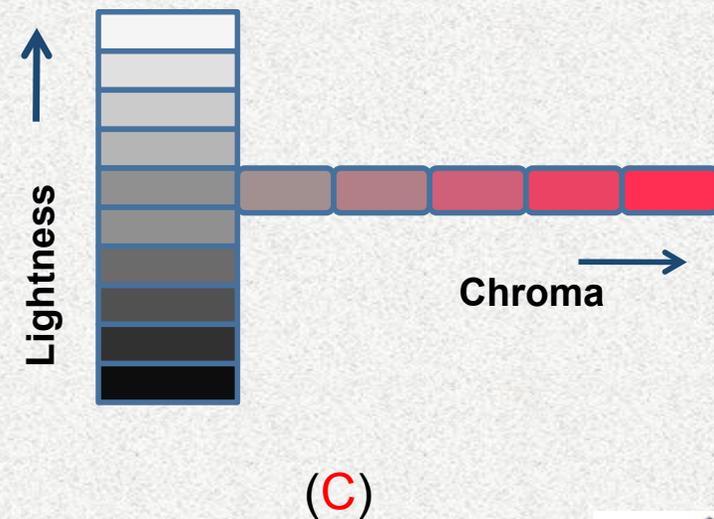
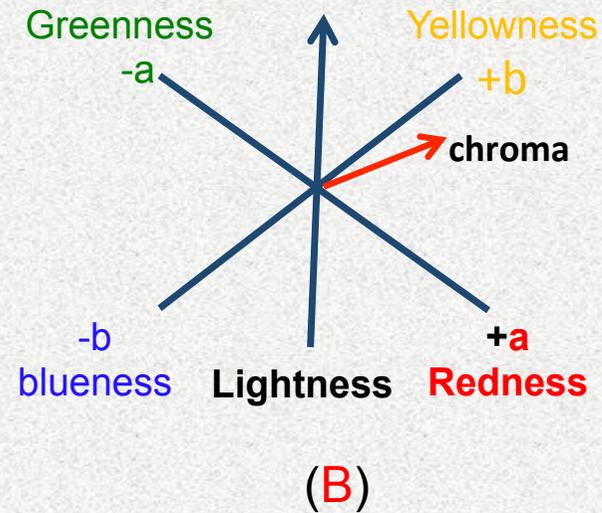
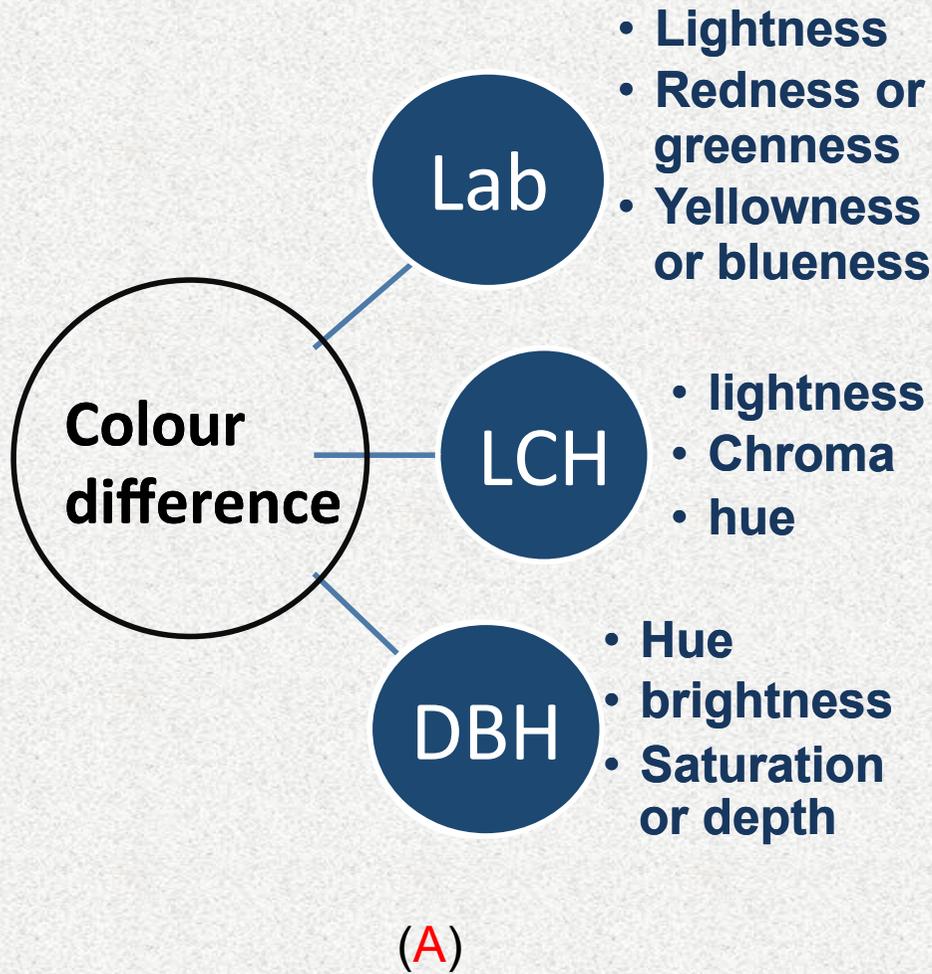


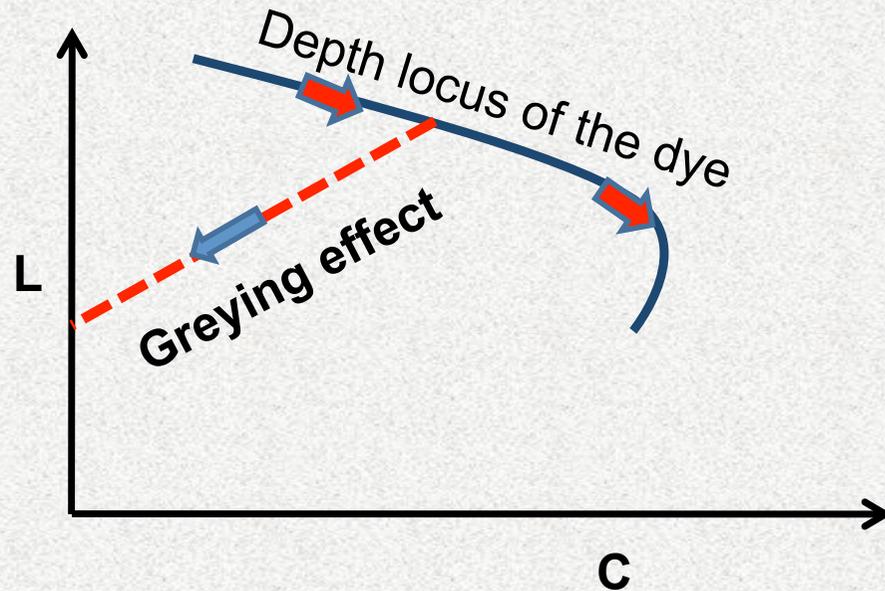
Development of an Algorithm to Convert Colorimetric variables of ΔL^* , ΔC^* ΔH^* to Dyers' Variables of Differences in Depth, Brightness and Hue

Salma Farooq
*School of Textiles and Design,
Heriot-Watt University, UK
Sf81@hw.ac.uk*

Colour difference and its partitioning



Relationship between dyers variables and colorimetric variables



$$\Delta L + \Delta C = \Delta D$$

$$\Delta L + \Delta C = \Delta B$$

- change in concentration of the dye is always accompanied with both the change in lightness and chroma.
- Addition of grey to the dyeing result in decrease of lightness and chroma.

Interpretation of LCh values. An Example

- Your target colour

$$L^* = 63 \quad C^* = 24$$

$$h = 45^\circ$$

- Your batch

$$L^* = 65 \quad C^* = 25$$

$$h = 45^\circ \quad \Delta E = 2.00$$

COLORIMETRIC OUTPUT

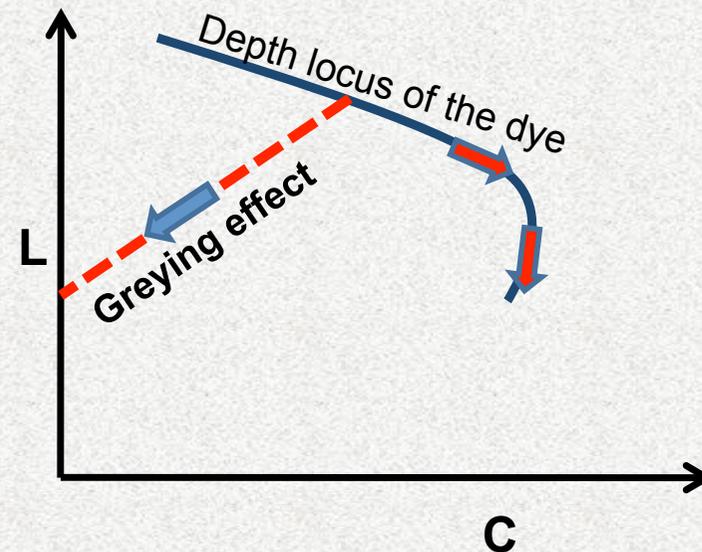
$$\Delta L = 2 \quad \Delta C = 1$$

- Instruction is decrease L^* and C^* - **but how?**

DYERS' OUTPUT

Batch is **thinner**

- Instruction is decrease the concentration



- **It is therefore necessary to inter-relate the output of the colorimetric variables to the dyers' variables to get maximum advantages of colorimetry**
- **The WSF algorithm developed in this work defines a systematic way of predicting the change in depth and change in brightness by computing the variation in the colorimetric components of colour difference (ΔC , ΔL) throughout the colour space.**

WSF Algorithm

Generation of the equi-depth line passing through the standard



Adjustment of dye strength of batch till it intersects the equi-depth line of the standard



Computation of difference in depth, brightness and hue of standard and batch

WSF Algorithm- How to generate Equi-Depth line

- Six surfaces of constant visual depth ($2/1$, $1/1$, $1/3$, $1/6$, $1/12$, $1/25$) defined numerically and mapped into CIELAB color space has been reported as WSI algorithm earlier.
- WSI algorithm was based upon predicting the lightness that colours of given chroma should have to be of equal depth, around the hue circle.

WSF Algorithm- How to generate Equi-Depth line

Conic equation was fitted to predict the lightness of the sample

$$k_1L^{*2} + k_2C^{*2} + k_3L^* + k_4L^*C^* + k_5C^* + k_6 = 0$$

$$L^* = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$a = k_1$$

$$b = k_3 + k_4C^*$$

$$c = k_2C^{*2} + k_5C^* + k_6$$

WSF Algorithm- How to generate Equi-Depth line

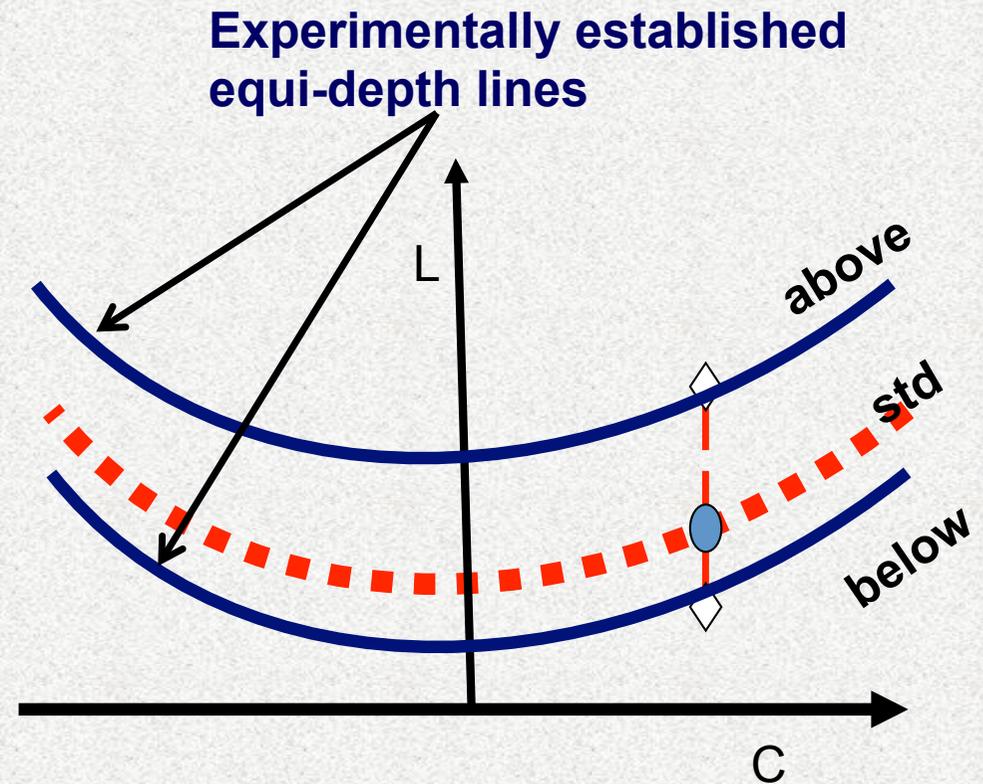
$$k_{1 \text{ std}} = k_{1 \text{ below}} + \Delta k_1$$

$$\Delta k_1 = \Delta L_1 / \Delta L_t * \Delta k_t$$

$$\Delta k_t = (k_{\text{above}} - k_{\text{below}})$$

$$\Delta L_t = (L_{\text{above}} - L_{\text{below}})$$

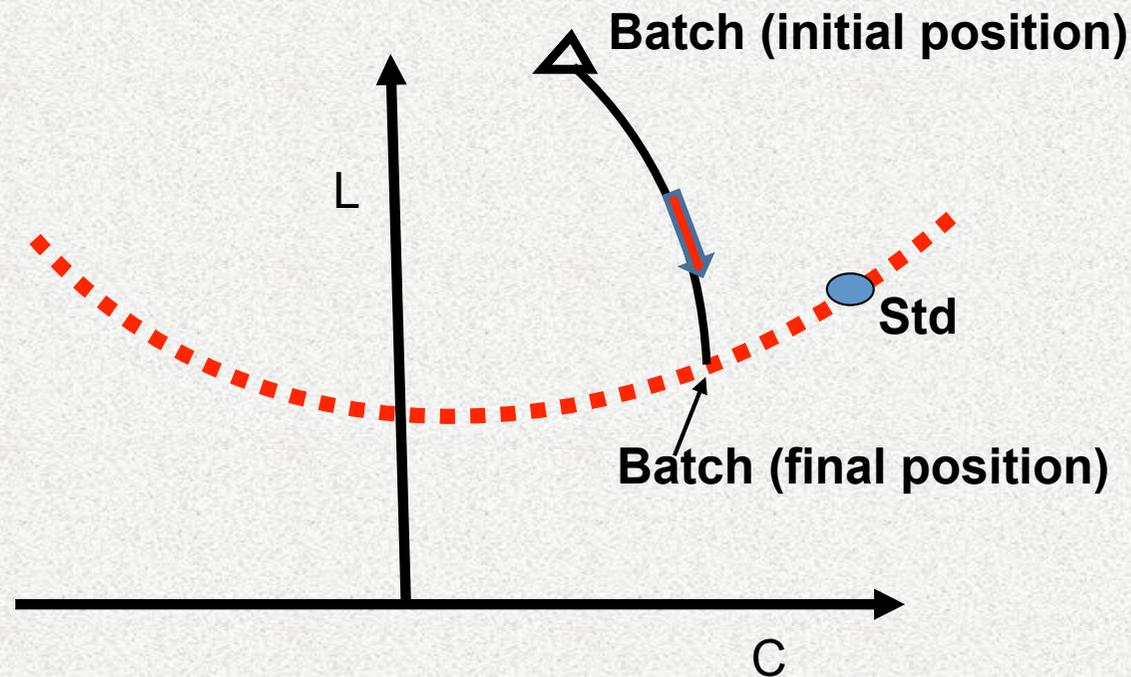
$$\Delta L_1 = (L_{\text{std}} - L_{\text{below}})$$



$$k_1 L^{*2} + k_2 C^{*2} + k_3 L^* + k_4 L^* C^* + k_5 C^* + k_6 = 0$$

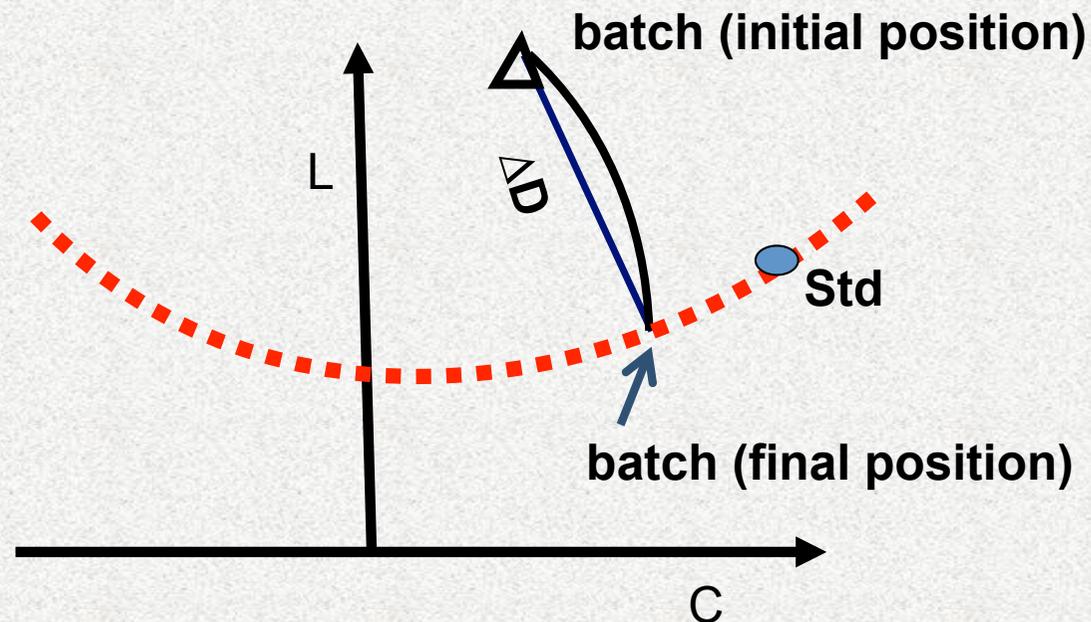
WSF Algorithm-prediction of batch strength relative to standard

- The K/S values of the batch are either increased or decreased, until its depth becomes equal to that of standard.



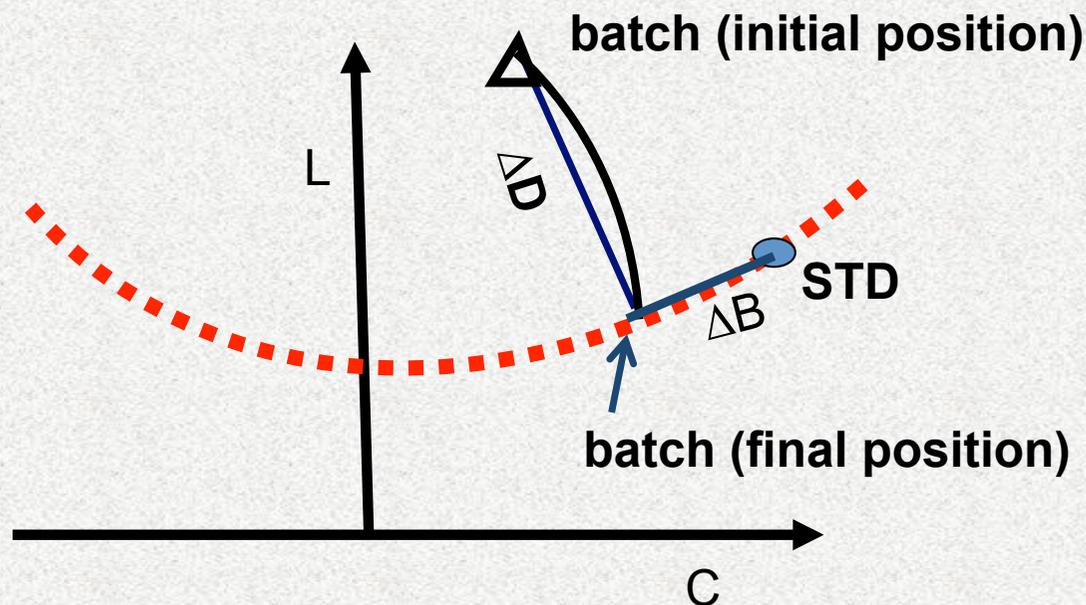
Computation Of Difference In Depth and its verbal description

- ΔD is the linear distance of the batch from its initial position to its final position
- Batch is **thinner** If the **concentration** of the batch **increases** to intersect the depth line of the standard, and vice versa



Computation Of Difference In Brightness and its verbal description

- ΔB is the linear distance between the location of the batch on the standard's equi-depth line and the location of the standard.
- The batch is **flatter** if its **chroma** on the equi - depth line of the standard is **lower** than the chroma of the standard, and vice versa



Statistical Analysis

- **39 pairs of samples showing small/medium colour differences of between 0.3 – 3.0 CIELAB units were prepared at different regions of the colour space.**
- **Each of the 39 sample pairs was assessed by a professional colourist. The colourist's decisions were made in terms of the percentage contribution of depth, brightness and hue to the overall colour difference seen.**
- **The differences in depth, brightness and hue of each of the pairs were computed using the WSF algorithm and also the DBH model**

Statistical Analysis

Correlation with visual assessment and with DBH

	$r (\Delta D)$	$r (\Delta B)$
WSF VS DBH	0.964	0.595
DBH VS VISUAL	0.519	0.323
WSF VS VISUAL	0.5304	0.138

Thank you